

# The temperature-scanning plug flow reactor (TSPFR) applied to complex reactions—Oxidative dehydrogenation of propane as an example

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## Abstract

The temperature-scanning plug flow reactor (TSPFR) enables the investigation of kinetics of chemical reactions over a wide temperature range in a relatively small time of operation. The experimental data obtained by this approach can be used to calculate the reaction rate of each component of the reactant mixture for a given set of conditions. The oxidative dehydrogenation of propane by a  $V_2O_5/\gamma-Al_2O_3$  catalyst was used for illustration. As this reaction is highly exothermic some limitations of the approach had to be considered.

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## 1. Introduction

Reliable kinetic data are of outstanding importance in reactor design and optimization. Inaccurate kinetic data spoil any reactor modelling. Kinetic measurements are very time consuming and involved. Therefore, it is desirable to introduce more efficient approaches in kinetic experimentation. In 1997, Wojciechowski and co-workers published a series of articles about the temperature-scanning reactor (TSR) [1–3], which allows to perform kinetic experiments in fully automated reactors in a far shorter time than in conventional devices. According to some industrial announcements, the TSR could accelerate measurements by a factor of up to ten. A major problem is the data evaluation algorithm, which has not been described in detail in the original paper by Wojciechowski [1]. Liebner et al. [4] developed an algorithm for effective evaluation of kinetic data of the temperature-scanning reactor and executed experimental tests on this reactor by employing the ammonia synthesis reaction. The reactor, combined with an appropriate mode of operation and approach of data evaluation, gave reliable values of reaction

rates for non-isothermal reactor operation in an integral range of conversion and a range of conversion including thermodynamic equilibrium, respectively. Thus, a large amount of data can be obtained leading to a well-founded basis of kinetic modelling. Kolkowski et al. [5] discussed sources of error in this type of reactor. The influence of heat transport phenomena on the reaction rate data obtained by the temperature-scanning plug flow reactor (TSPFR) was investigated by means of simulation. The main advantages of the TSPFR can be summed up like this:

- fast kinetic investigations over a large temperature range are possible;
- automation of the entire device is possible;
- a large amount of data can be monitored in a rather short time;
- the TSPFR is simple to implement and requires only standard hardware.

Contrary to the ammonia synthesis, in the present paper a complex irreversible reaction was investigated by the TSPFR, namely the oxidative dehydrogenation of propane. This reaction is extremely exothermic, and should reveal supposable limitations of the TSPFR approach. Resorts from these limitations will be discussed.

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### Nomenclature

$Bi$	Biot number
$c$	concentration (mol/m <sup>3</sup> )
$D_{ax}$	axial dispersion coefficient (m <sup>2</sup> /s)
$d_i$	inner tube diameter (m)
$d_p$	pellet diameter (m)
$E_A$	activation energy (J/mol)
$h$	number of a certain measurement point
$k$	reaction rate constant (mol/(kg Pa s))
$k_o$	overall heat transfer coefficient (W/(m <sup>2</sup> K))
$K_{O_2}$	adsorption constant of oxygen (Pa <sup>-1.5</sup> )
$l$	equivalent length (m)
$L$	length of the reactor (m)
$m_{cat}$	mass of catalyst (kg)
$\dot{n}$	molar flow rate (mol/s)
$N_a$	reaction number
$N_i$	number of a certain residence time
$N_j$	number of a temperature interval
$p$	pressure (Pa)
$r$	radius inside the catalyst packing (m)
$r^*$	collocation point (radius) (m)
$r_i$	inner tube diameter (m)
$r_{Ri}$	reaction rate of reaction $i$ (mol/(kg s))
$r_{TS}$	reaction rate from experiments (mol/(kg s))
$s$	residence time (s)
$t$	time (s)
$u_{LR}$	superficial gas velocity (m/s)
$T$	temperature (K)
$T^*(r^*)$	temperature at the collocation radius $r^*$ (K)
$\dot{V}$	volumetric flow (m <sup>3</sup> /s)
$x$	molar fraction

#### Greek letters

$\delta(t)$	see Eq. (2)
$\lambda_{cat}$	heat conductivity of catalyst (W/(m K))
$\nu_{ij}$	stoichiometric constant of component $i$ in reaction $j$

## 2. Experimental

The experimental set-up is presented in Fig. 1. The experiments were carried out in a quartz tube reactor. The reactor was placed in an oven with rapidly circulating air. The outer surface temperature of the reactor should be the same at any position. The oven temperature was controlled by micro-processor controllers. The flows of the inlet gases were controlled by electronic mass flow meters (Bronkhorst F 201 C). Gases of better than 99.9% purity were used. For gas analysis, a micro-gas chromatograph (Varian Chrompack CP 2002) was applied. The sampling by the GC inlet system was done at the exit of the catalyst bed, i.e., inside the reactor tube. A carefully heated capillary and GC inlet system

was used to avoid condensing of reaction products. As catalyst  $V_2O_5/\gamma-Al_2O_3$  was chosen as it provides high propene yields at moderate temperatures. Furthermore, this catalyst is robust and can be regenerated. The catalyst was manufactured in the following way: 0.822 g  $V_2O_5$  and 0.5 g polyvinyl acetate were slowly added to a stirred solution of 2 g oxalic acid in 130 ml  $H_2O$  at 75 °C. The clear liquid is cooled down to room temperature and mixed with 5 g  $\gamma-AlO(OH)$ . After having stirred this solution for 15 min,  $\gamma-Al_2O_3$  was slowly added. The catalyst was dried for 24 h at 60 °C, and then calcinated for 6 h at 600 °C in stagnant air. The catalyst has initially a green-yellow colour and turns to green, like chromium oxide, after usage. Its BET surface was 130 m<sup>2</sup>/g. XRD analysis showed only  $\gamma$ - and  $\delta$ - $Al_2O_3$  phases. The catalyst ( $V_2O_5/\gamma-Al_2O_3$  diluted with  $SiO_2$  particles (1:5) because of the high exothermicity of the reaction) has to be evenly distributed along the reactor in order to have a uniform effectiveness along the reactor. A feed of constant gas composition and flow is supplied to the reactor inlet. The inlet gas is heated according to a defined temperature program before entering the reactor. The reactants preheating unit is installed inside the oven. The temperature is recorded at the inlet and the outlet of the reactor. The gas composition is also measured at the outlet. After having run the temperature program, the reactor is cooled down to the temperature level of the previous run. During the cooling down period, the catalyst was regenerated by pure oxygen flowing through the catalyst bed. This resulted in a reproducible activity for each of the operated temperature ramps. Then, a different flow rate of the reactants is adjusted, and exactly the same temperature ramp is operated. The temperature of the surrounding air with which the reactor exchanges heat must be ramped in the same way, from the same starting temperature, in each run. This ensures that the driving forces for heat fluxes between the reactor and its surroundings are the same from run to run. This procedure is repeated for a defined number of different reactant volume flow rates, which correspond to different residence times inside the reactor. The TSPFR gives, without approximation or extrapolation, conventional multiplets of conversion/yields–rates–temperatures. After certain time intervals, data like experiment run time,  $t_i$ , oven temperature,  $T_{oven}$ , reactor inlet temperature,  $T_{in}$ , reactor outlet temperature,  $T_{out}$ , and the mole fractions,  $x_i$ , of all species in the outlet gas are measured. To make such data interpretable, the temperature ramping rate has to be such that the time between successive analyses is much shorter than the time required for a kinetically significant increment of temperature to be induced in the feed to the reactor. The pressure and the composition of the reactants have to be the same in all runs. Inside the reactor, plug flow conditions have to exist. As a consequence, there should be nearly no radial temperature profile in the catalyst bed. Hot spots have to be avoided. These conditions have to be checked. As the details of the TSPFR theory are given by Liebner et al. [4], only a few remarks about the data evaluation of the TSPFR will be given here. The foundation of the evaluation of kinetic data by means

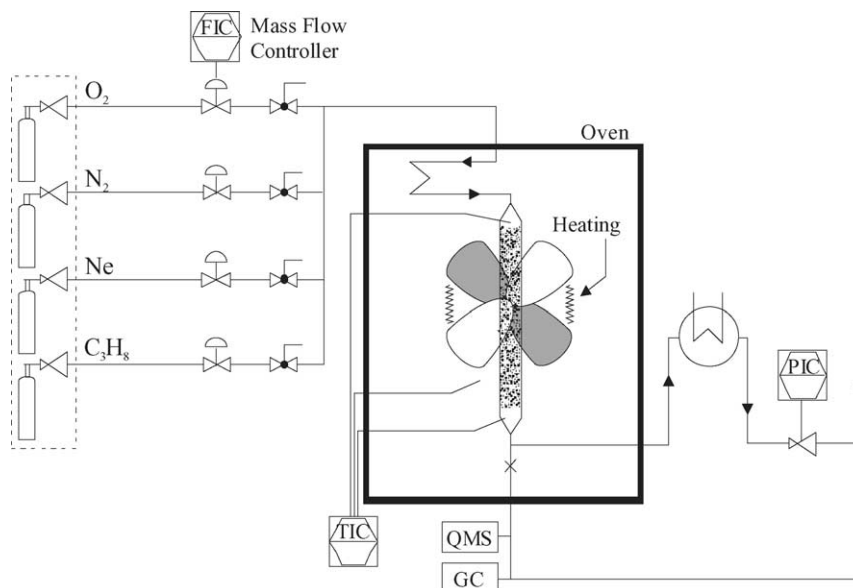


Fig. 1. Experimental set-up of the temperature-scanning plug flow reactor (TSPFR).

of the TSPFR approach starts with the material balance of an ideal stationary tubular reactor:

$$0 = -\frac{d(c_i \dot{V})}{dm_{\text{cat}}} + \sum v_{ij} r_j \text{ (mol/(kg s))} \quad (1)$$

To transfer this equation to a tubular reactor of constant length, whereby the residence time is varied for a constant catalyst mass, a factor  $\delta(t)$  is defined, which is the ratio of the volume flow rate at the exit of the reactor at time  $t$ ,  $\dot{V}_{\text{out}}(t)$ , to the volume flow rate at the reactor inlet at that time,  $\dot{V}_{\text{in}}(t-s)$ . The catalyst contact time,  $s$ , is the actual residence time of a volume element of the fluid in the catalyst packing. That means  $\delta(t)$  is a measure for the relative volume change of a volume element owing to temperature change and chemical reaction.

$$\delta(t) = \frac{\dot{V}_{\text{out}}(t)}{\dot{V}_{\text{in}}(t-s)} \quad (2)$$

Inserting Eq. (2) into Eq. (1) gives:

$$0 = -\dot{V}_{\text{in}}(t-s) \frac{d(c_i \delta(t))}{dm_{\text{cat}}} \Big|_{T_{\text{in}}} + \sum v_{ij} r_j \text{ (mol/(kg s))} \quad (3)$$

Note that  $\dot{V}_{\text{in}}(t-s)$  is constant for a constant reactor inlet temperature. In order to determine  $\delta(t)$ , the volume flow rates at the reactor inlet and outlet have to be measured. In the actual experiment, the volume flow rates,  $\dot{V}_{\text{ref}}$ , are measured under ambient conditions, which are the reference ( $P_{\text{ref}} = 1$  bar,  $T_{\text{ref}} = 298$  K). By means of the perfect gas law (or an equation of state, if necessary), this flow rate can be converted into the inlet and outlet conditions of the reactor, as the temperatures, pressures and compositions of the gases are known. In order to include the volume change owing to chemical reaction, an inert component is added to the reactants. The ratio of the

mole fraction at the reactor inlet to the mole fraction at the outlet gives the change of the volume flow rate owing to reactions. The outlet volume flow rate is multiplied with this ratio:

$$\begin{aligned} \dot{V}_{\text{out}}(t) &= \dot{V}_{\text{ref}} \frac{P_{\text{ref}}}{P_{\text{out}}(t)} \frac{T_{\text{out}}(t)}{T_{\text{ref}}} \frac{x_{\text{in,inert}}}{x_{\text{out,inert}}} \\ &= \dot{V}_{\text{ref}} \frac{P_{\text{ref}}}{P_{\text{out}}(t)} \frac{T_{\text{out}}(t)}{T_{\text{ref}}} \frac{\dot{n}_{\text{out}}(t)}{\dot{n}_{\text{in}}(t)} \text{ (m}^3/\text{s)} \end{aligned} \quad (4)$$

$$\dot{V}_{\text{in}}(t-s) = \dot{V}_{\text{ref}} \frac{P_{\text{ref}}}{P_{\text{in}}} \frac{T_{\text{in}}(t-s)}{T_{\text{ref}}} \text{ (m}^3/\text{s)} \quad (5)$$

Eqs. (4) and (5) are inserted into Eq. (2):

$$\delta(t) = \frac{P_{\text{ref}}}{P_{\text{out}}(t)} \frac{T_{\text{out}}(t)}{T_{\text{in}}(t-s)} \frac{x_{\text{in,inert}}}{x_{\text{out,inert}}(t)} \quad (6)$$

By means of Eqs. (5) and (6) one can simplify Eq. (3). Additionally a residence time, which is related to the catalyst mass, is introduced:

$$d\tau_{\text{cat}} = \frac{dm_{\text{cat}}}{\dot{V}_{\text{ref}}} \text{ (kg s/m}^3\text{)} \quad (7)$$

Finally, one obtains an equation for the data evaluation of TSPFR experiment:

$$\begin{aligned} \frac{\dot{n}_{\text{ref}}}{\dot{V}_{\text{ref}}} x_{\text{in,inert}} \frac{d}{d\tau_{\text{cat}}} \left( \frac{x_i(t, \tau_{\text{cat}})}{x_{\text{out,inert}}(t, \tau_{\text{cat}})} \right) \Big|_{T_{\text{in}}} \\ = \sum v_{ij} r_j \text{ (mol/(kg s))} \end{aligned} \quad (8)$$

All the data required in Eq. (8) are obtained from the TSPFR experiment. The experimental conditions employed in the present investigations are given in Table 1. The details of data evaluation are given by Liebner et al. [4].



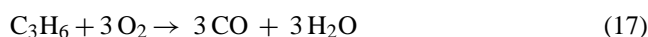
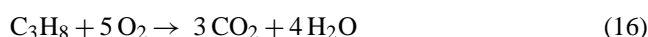
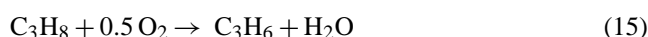
Table 3  
Reactant concentrations corresponding to Figs. 2–4

Reactant concentrations (inlet) (mol%)				Residence time (kg s/m <sup>3</sup> )					
				Reference volume flow rate (l <sub>N</sub> /min)					
Ne	N <sub>2</sub>	C <sub>3</sub> H <sub>8</sub>	O <sub>2</sub>	(□)	(○)	(△)	(◇)	(▽)	(◁)
5.0	87.50	5.0	2.5	15.0	18.8	21.4	25.0	30.0	37.5
				1.0	0.9	0.8	0.7	0.6	0.5

higher reactants content in the reactant gas mixture leads to such a high exothermicity that the data could not be evaluated in the TSPFR frame. This reveals some limitations of the TSPFR approach for highly exothermic reactions. Because of the total oxidation of propane, oxygen was consumed very fast. For this reason, the rate of reaction of oxygen is four times faster than propane. The products were propene, carbon monoxide, carbon dioxide, water, and traces of ethane, ethene and methane. Propene and carbon monoxide were formed at an amount of 0.5 mol% each. Up to a temperature of 680 K, the rate of reaction is moderate. Between 680 and 700 K, the rate of reaction increases sharply to a maximum at about 730 K and decreases at higher temperatures due to oxygen limitation.

In order to evaluate the measured data, details of the reaction mechanism have to be known. Depending on the catalyst, sometimes a hypothetical reaction mechanism will do. Grabowski et al. [8] concluded by means of transient experiments that the first step of propane conversion follows an Eley–Rideal mechanism. Propane reacts directly from the

gas phase with the adsorbed oxygen on the catalyst. Chen et al. [9] showed that propane is dehydrogenated to propene, and in parallel to the total oxidation of propane to carbon dioxide occurs. Carbon monoxide is exclusively created by oxidation of propene. Carbon dioxide is generated by oxidation of propane and propene. Based on these findings, the following reaction scheme was employed:



The first equation corresponds to the oxidative dehydrogenation of propane. The second equation assumes that carbon dioxide is primarily formed by oxidation of propane. Oxidation of propene to carbon monoxide is given in the third equation. Some other groups investigated the kinetics of ODH of propane (see, for example, Argyle et al. [10] and Late and Blekken [11], and the literature cited therein). Based on these reactions, three Eley–Rideal-type rate equations were

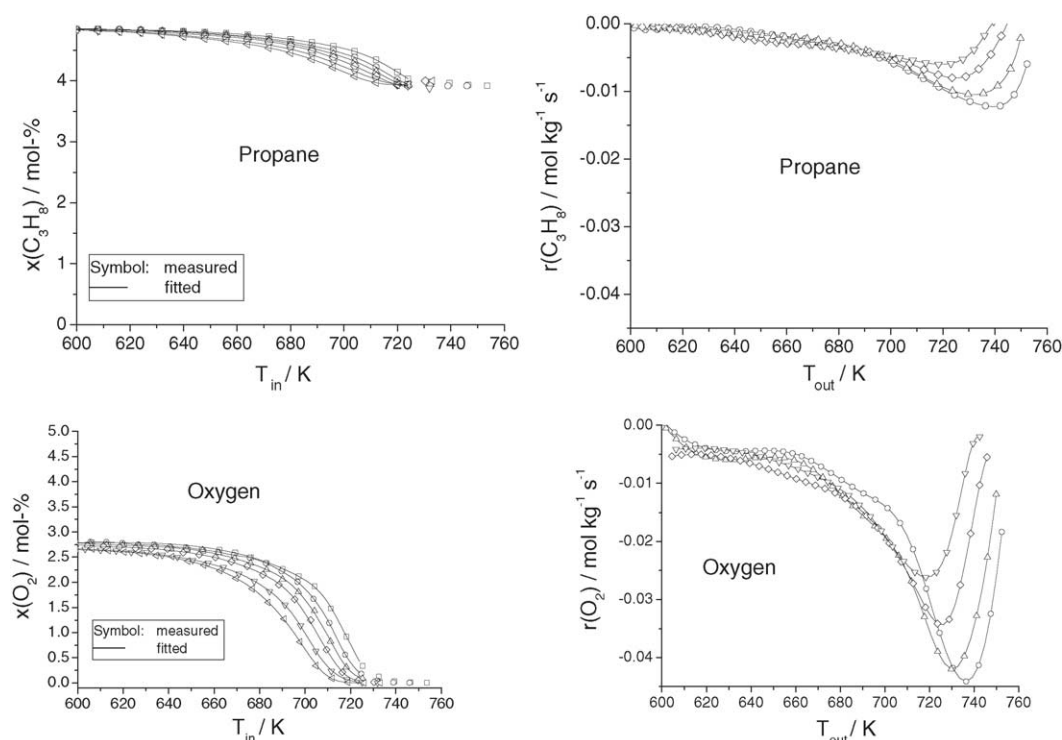


Fig. 3. Reactant concentrations and reaction rates as a function of the inlet and outlet temperature, respectively.

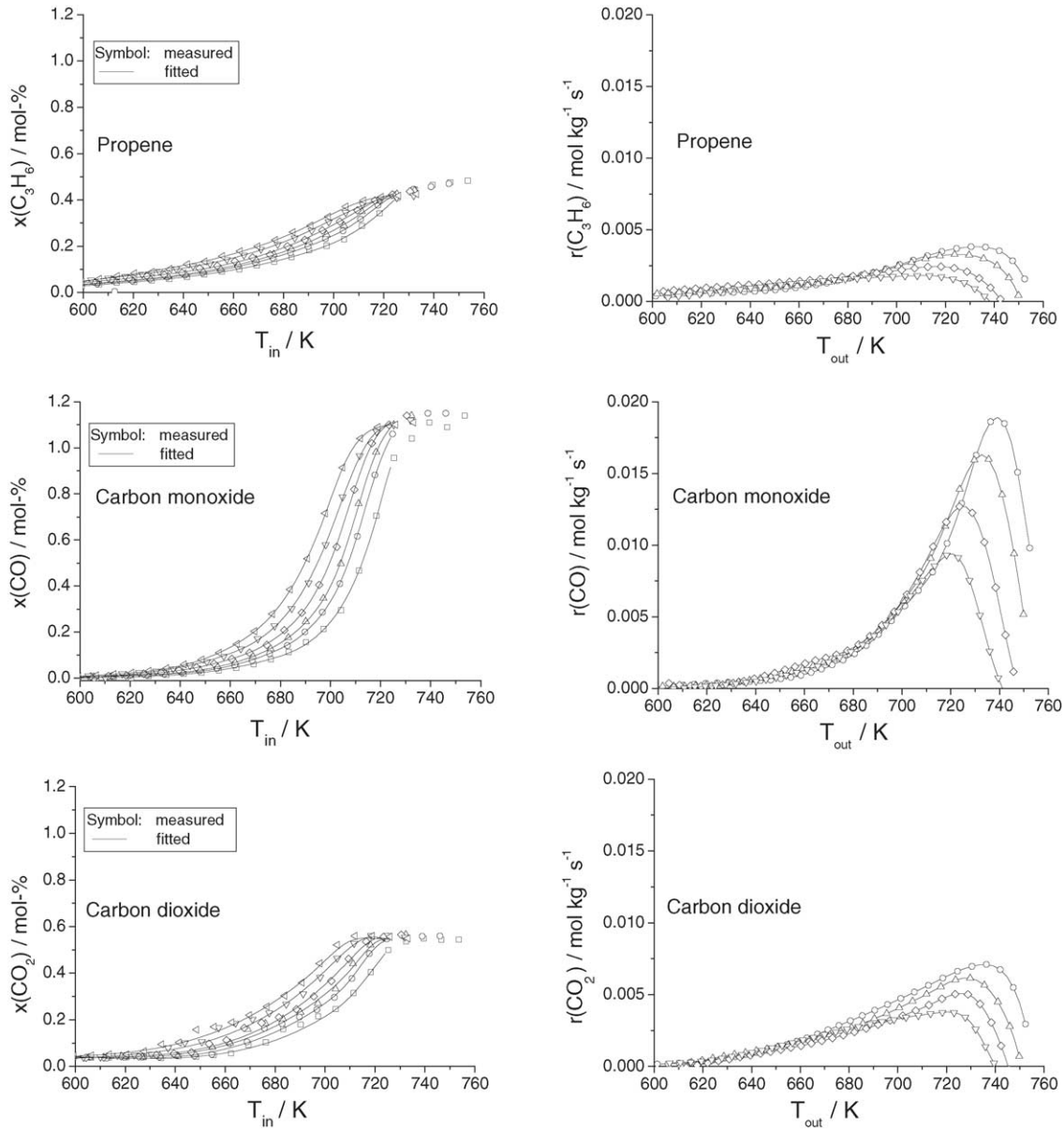


Fig. 4. Product concentration and reaction rates as function of the inlet and outlet temperature, respectively.

introduced:

$$r_{R1} = \frac{k_1 K_{O_2} p_{C_3H_8} p_{O_2}^n}{1 + K_{O_2} p_{O_2}^m} \quad (\text{mol}/(\text{kg s})) \quad (18)$$

$$r_{R2} = \frac{k_2 K_{O_2} p_{C_3H_8} p_{O_2}^n}{1 + K_{O_2} p_{O_2}^m} \quad (\text{mol}/(\text{kg s})) \quad (19)$$

$$r_{R3} = \frac{k_3 K_{O_2} p_{C_3H_6} p_{O_2}^n}{1 + K_{O_2} p_{O_2}^m} \quad (\text{mol}/(\text{kg s})) \quad (20)$$

Amongst the experimental reaction rates,  $r_{TS}$ , the following relations exist:

$$r_{TS, r_{R1}} = r_{TS, C_3H_6} + \frac{r_{TS, CO}}{3} \quad (\text{mol}/(\text{kg s})) \quad (21)$$

$$r_{TS, r_{R2}} = \frac{r_{TS, CO_2}}{3} \quad (\text{mol}/(\text{kg s})) \quad (22)$$

$$r_{TS, r_{R2}} = \frac{r_{TS, CO}}{3} \quad (\text{mol}/(\text{kg s})) \quad (23)$$

The parameters of these equations were determined by means of the experimental rates,  $r_{TS}$ . The following performance index was minimized by a sequential quadratic programming (SQP) algorithm (NAG library, program E04UCF):

$$Q_r = \sum_{h=1}^{N_j(N_i-2)} (\ln(r_{k, TS, h}) - \ln(r_h))^2 \stackrel{!}{=} \text{MIN} \quad (24)$$

$$r_h = \sum_{a=1}^{N_a} v_{ka} r_a \quad (\text{mol}/(\text{kg s})) \quad (25)$$

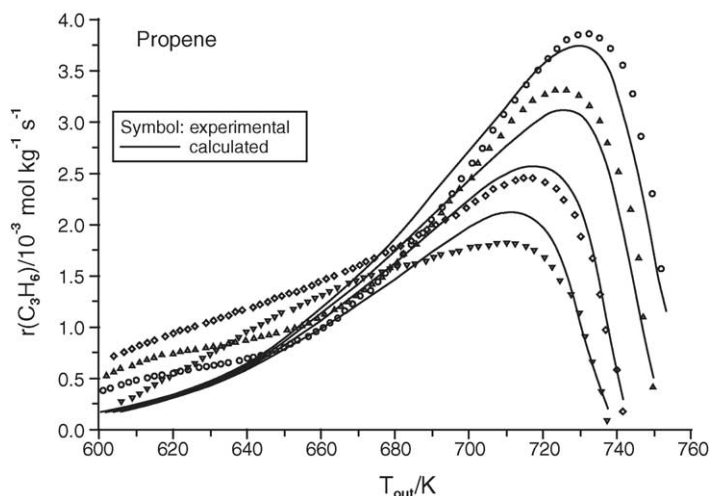


Fig. 5. Reaction rate of propene as a function of temperature.

$$r_a = f(x, T, P, k(t), K(T)) \text{ (mol/(kg s))} \quad (26)$$

$$k(T) = k_o \exp\left(\frac{-E_A}{RT}\right) \quad (27)$$

The dimension of  $k(T)$  depends on the reaction. In our case, it is  $k \text{ mol}/(\text{kg Pa s})$ . The results are given in Table 4. Besides Eqs. (18)–(20), Langmuir–Hinshelwood equations were used, but Eqs. (18)–(20) gave the lowest mean square deviation. A Mars-van-Krevelen kinetics was not tested (see, e.g., [11]). The carbon balance showed no coke formation up to 730 K. Above this temperature, some coke formation was observed. Argyle et al. [10] found an activation energy for propane ODH and propane combustion of  $\sim 115 \pm 20 \text{ kJ/mol}$  and an apparent activation energy for the propene combustion of 60–90 kJ/mol. Similar values were obtained by Late and Blekken [11]. The experimental reaction rates were compared with the calculated rates whereby the fitted parameters were used. The deviations are below  $\pm 15\%$ . The fitted data can be employed for a check of the calculated reaction rates of propene. According to Eq. (15), propene is formed from propane, and is oxidized to carbon monoxide (Eq. (17)). The

rate of reaction of propene is given by (Eqs. (15)–(17)):

$$r_{C_3H_6} = r_1 - r_3 \text{ (mol/(kg s))} \quad (28)$$

The results are given in Fig. 5. The experimental data are identical to the propene data in Fig. 4. In the region between 600 and 660 K, there is a considerable deviation between measurements and calculations. This is the result of imprecision of concentration measurements in this temperature range, as the reaction was not yet ignited. The propene concentration in this temperature range is about 0.2 mol% (compare Fig. 4). Above 680 K, measurements and calculated reaction rates coincide well. This result confirms that the measurements and the reaction rates calculated from them are consistent. Likelihood regions of kinetic parameters were also calculated. For this purpose, the kinetic parameters occurring in the reaction rate equations were pair wise varied, and the deviations from the minimum of the performance index (see Eq. (24)) were plotted at 10, 20 and 30%. There are five possible combinations for each of the three reactions (see Eqs. (15)–(17)). It was found that the deviations are largest for cases where the parameters are coupled as products of the Arrhenius equation. This holds for  $k_{1,2,3}$  and  $K_{O_2}$ .

Not in the present example, but in principle a very high exothermicity of reactions may lead to difficulties within the TSPFR scheme because of too large radial temperature profiles. For such a case, one could redesign the reactor. Two coaxial cylinders could be used where the inner cylinder and the annulus are filled with the same catalyst. By employing a proper volumetric flow rate of the reactants in the inner tube and the annulus, nearly the same temperature profiles are created inside the inner tube and the annulus, which minimizes the uneven heat flow from the inner tube to the surrounding gas in the oven. Whether this modification is sufficient, has to be checked. Parallel reactors can further accelerate the TSPFR measurements.

Table 4  
Kinetic parameters of the reactions (Eqs. (18)–(20)) by fitting and optimizing the experimental data

Constant	Parameters	Value
$k_1$	$k_{1,0}$	6.90 mol/(kg s Pa)
	$E_{A,1}$	$104.68 \pm 15 \text{ kJ/mol}$
$k_2$	$k_{2,0}$	5.70 mol/(kg s Pa)
	$E_{A,2}$	$83.70 \pm 20 \text{ kJ/mol}$
$k_3$	$k_{3,0}$	8.66 mol/(kg s Pa)
	$E_{A,3}$	$79.65 \pm 20 \text{ kJ/mol}$
$K_{O_2}$	$k_{o2,0} \times 10$	$4.02 \text{ Pa}^{-1.5}$
	$E_{A,O_2}$	49.71 kJ/mol
$n, m$	–	1.50

#### 4. Conclusion

In the present investigation, the concept of the TSPFR was employed to a complex reaction system. Like the case of ammonia formation from hydrogen and nitrogen, the kinetics of oxidative dehydrogenation of propane could be described satisfactorily by the TSPFR approach, provided that the propane content in the reactant mixture was kept below a certain value. For extremely exothermic reactions, the TSPFR approach cannot be employed without modifications. Nevertheless, in general a large amount of data can be obtained in a rather short time, leading to a well-founded basis of kinetic modelling.

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